

Protostellar collapse: radiative and magnetic feedbacks on small scale fragmentation.

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ABSTRACT

Context. It is established that both radiative transfer and magnetic field have a strong impact on the collapse and the fragmentation of prestellar dense cores, but no consistent calculation exists yet at such scales.

Aims. We perform the first Radiation-Magneto-HydroDynamics numerical calculations at a prestellar core scale.

Methods. We present original AMR calculations including magnetic field (in the ideal MHD limit) and radiative transfer, within the Flux Limited Diffusion approximation, of the collapse of a $1 M_{\odot}$ dense core. We compare the results with calculations performed with a barotropic EOS.

Results. We show that radiative transfer has an important impact on the collapse and the fragmentation, through the cooling or heating of the gas, and is complementary of the magnetic field. A larger field yields a stronger magnetic braking, increasing the accretion rate and thus the effect of the radiative feedback. Even for a strongly magnetized core, where the dynamics of the collapse is dominated by the magnetic field, radiative transfer is crucial to determine the temperature and optical depth distributions, two potentially accessible observational diagnostics. A barotropic EOS cannot account for realistic fragmentation. The diffusivity of the numerical scheme, however, is found to strongly affect the output of the collapse, leading eventually to spurious fragmentation.

Conclusions. Both radiative transfer and magnetic field must be included in numerical calculations of star formation to obtain realistic collapse configurations and observable signatures. Nevertheless, the numerical resolution and the robustness of the solver are of prime importance to obtain reliable results. When using an accurate solver, the fragmentation is found to always remain inhibited by the magnetic field, at least in the ideal MHD limit, even when radiative transfer is included.

Key words. magnetohydrodynamics (MHD), radiative transfer - Stars: low mass, formation - ISM: kinematics and dynamics, clouds

1. Introduction

Understanding star formation is one of the most challenging problems in contemporary astrophysics and numerical calculations provide a useful approach to investigate it thoroughly. Thanks to the steadily increasing computer performances, numerical calculations can integrate more and more physical processes. Among these latter, the coupling between matter and radiation is a major issue. Up to the formation of the first Larson core (Larson 1969), the accreting gas can freely radiate into space and is nearly isothermal (optically thin regime). Once the gas becomes dense enough ($\rho > 10^{-13} \text{ g cm}^{-3}$), the radiation is trapped and the gas starts to heat up (optically thick regime). The transition between these two regimes controls the collapse and the fragmentation of the cloud. The cooler the gas, the more important the fragmentation. Another key issue in star formation is the role of the magnetic field, as dense cores are observed to exhibit coherent magnetic structures (e.g. Heiles & Crutcher 2005).

Several authors have investigated the impact of radiation (Boss et al. 2000; Whitehouse & Bate 2006; Attwood et al. 2009; Krumholz et al. 2007; Bate 2009; Offner et al. 2009) and of magnetic field (e.g. Mellon & Li 2009; Banerjee &

Pudritz 2006; Hennebelle & Teyssier 2008; Machida et al. 2008; Price & Bate 2007, 2008) on the star formation process. So far, however, only Price & Bate (2009) have performed calculations with both magnetic field and radiative feedback, with an SPH method. Yet, these calculations explore relatively large scales. In this Letter, we present the first full Radiation-Magneto-HydroDynamics (RMHD) calculations of the protostellar collapse at small scales. We investigate in detail the impact of both magnetic field (in the limit of ideal MHD) and radiative feedback on the fragmentation process and on the launching of outflows. The results are compared with the ones obtained with a barotropic equation of state (EOS), that crudely mimics the transition from the isothermal to adiabatic regime, in order to assess the importance of a proper treatment of radiative transfer on the collapse.

2. Numerical method and initial conditions

We use the RAMSES code (Teyssier 2002) based on a Eulerian formalism (grid based method with Adaptive Mesh Refinement). We solve the transfer equations in the Flux Limited Diffusion (FLD, Minerbo 1978) in the comoving frame (fluid frame) to evaluate the radiative quantities. The ideal MHD equations are integrated using an unsplit second-order Godunov

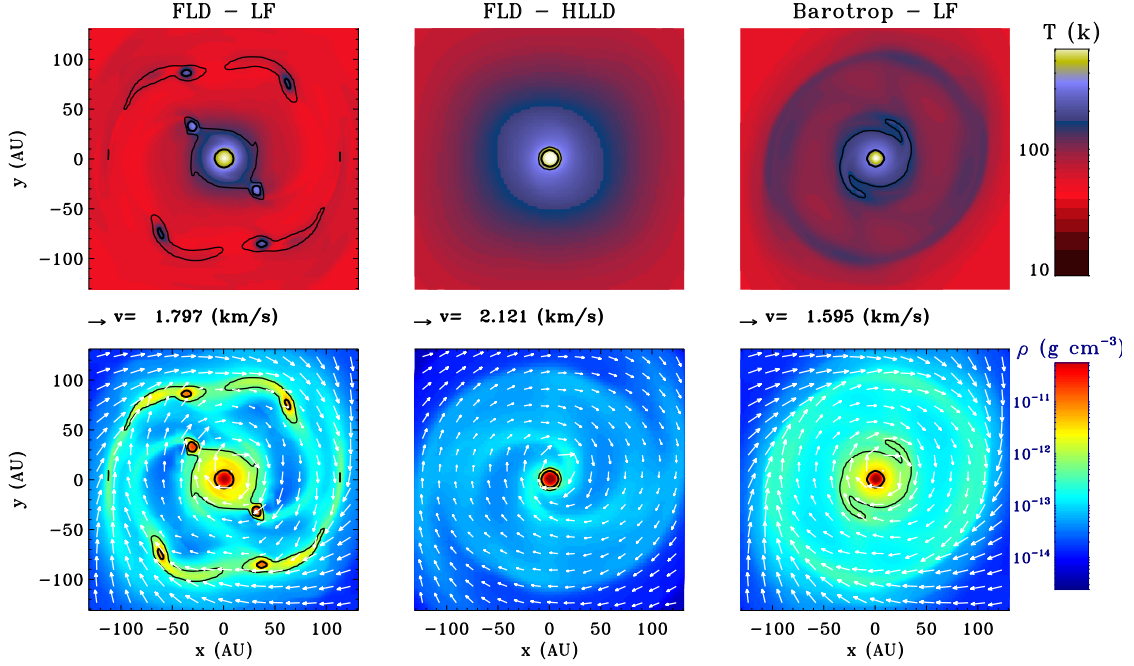


Fig. 1. Case $\mu = 20$: Density and temperature maps in the equatorial plane at time $t = 38.6$ kyr: FLD approximation with LF (*left*), FLD with HLLD (*middle*) and with the barotropic EOS (*right*).

scheme (Fromang et al. 2006). Coupling terms between matter and radiation, as well as radiation transport, are integrated implicitly in order to handle the very short heating, cooling and diffusion time scales. Details on the numerical method and its implementation will be presented in a forthcoming paper.

Calculations have been performed using either the rather diffusive Lax Friedrich (LF) Riemann solver or the more accurate HLLD Riemann solver (Miyoshi & Kusano 2005). Following up on former studies (Commerçon et al. 2008), we impose at least 10 cells per Jeans length as a grid refinement criterion (parameter N_J). The initial resolution of the grid contains 64^3 grids. We use the low temperature opacities of Semenov et al. (2003), parametrized as functions of the gas temperature and density. In contrast, the non radiative calculations have been performed with a barotropic EOS $P/\rho = c_{s0}^2[1 + (\rho/\rho_{ad})^{\gamma-1}]$, where $\rho_{ad} = 2.3 \times 10^{-13} \text{ g cm}^{-3}$ is the critical density at which the gas becomes adiabatic, γ (set up to 5/3) is the adiabatic index and c_{s0} the isothermal sound speed.

We adopt initial conditions, similar to those chosen in previous studies (e.g. Commerçon et al. 2008). We consider a uniform-density sphere of molecular gas, rotating about the z -axis with a uniform angular velocity. In the present study, the prestellar core mass is fixed at $M_0 = 1 M_\odot$ and the temperature at 11 K, which corresponds to $c_{s0} \sim 0.19 \text{ km s}^{-1}$. To promote fragmentation, we use an $m = 2$ azimuthal density perturbation with an amplitude of 10%. The magnetic field is initially uniform and parallel to the rotation axis. The strength of the magnetic field is expressed in terms of the mass-to-flux over critical mass-to-flux ratio $\mu = (M_0/\Phi)/(M_0/\Phi)_c$. The initial energy balance is determined by two dimensionless parameters, namely the ratio of the thermal over gravitational energies $\alpha = 0.37$, and rotational over gravitational energies $\beta = 0.045$. The corresponding free-fall time is $t_{ff} \sim 33 \text{ kyr}$.

3. Results

3.1. Case $\mu = 20$

We first present the results for $\mu = 20$, i.e. a weakly magnetised core. We compare FLD calculations performed with the two Riemann solvers (LF or HLLD) with calculations performed with the barotropic EOS and the LF solver. The grid refinement criterion is $N_J = 15$. Performing similar barotropic calculations, Hennebelle & Teyssier (2008) do not report any fragmentation.

Figure 1 portrays temperature (*top*) and density (*bottom*) maps in the equatorial plane for the three aforementioned calculations at the same time $t \sim 38 \text{ kyr}$. The black contours represent the transition between the optically thin and thick regions (thin contour) and the quasi adiabatic regions. The FLD case with the LF solver yields a multiple fragmentation, with a central fragment of mass $5.2 \times 10^{-2} M_\odot$ and several (depending on the time and resolution) orbiting fragments of mass $\sim 2 - 4 \times 10^{-3} M_\odot$ with separations ranging from $\sim 40 \text{ AU}$ to $\sim 100 \text{ AU}$, whereas no fragmentation occurs in the two other cases. The orbiting fragments in the FLD-LF simulation are quite warm ($\sim 40 \text{ K}$) while the disk is cold ($\sim 11 \text{ K}$). In all the simulations, the central fragment ($T > 500 \text{ K}$) corresponds to an adiabatic region, where the gas cannot radiate away its compressional energy. In the barotropic case, the mass of the central fragment is $4.9 \times 10^{-2} M_\odot$. The outer parts of the disk formed are much denser and warmer than for the two other cases, even though the gas is optically thin and should cool off efficiently, as illustrated in the FLD-LF calculations. The corresponding values of the Toomre parameter and Jeans length are larger than in the FLD-LF case. Such heating, however, is spurious and reflects the approximate treatment of radiative cooling with a barotropic approximation, where temperature is set up by the density.

The most interesting case is the FLD case with the HLLD Riemann solver. No fragmentation occurs in that case. The matter falls onto a central core of mass $\sim 7.3 \times 10^{-2} M_\odot$. With this

less diffusive solver, the generation of a toroidal magnetic field is more efficient. The interplay of magnetic field lines and velocity gradients leads to the effective expansion of a magnetic “tower” in the vertical direction (Hennebelle & Fromang 2008). The first consequence of this more robust (less diffusive) solver is that the disc formed is less massive in the equatorial plane than with the LF solver.

Figure 2 shows the density, temperature and poloidal and toroidal magnetic field profiles in the z -direction at a distance of 10 AU from the center, for the three aforementioned calculations, at the same time. We have noted that the extent of the magnetic tower depends on (increases with) the resolution. The magnetic tower is less dense close to the equatorial plane, since the gas is spread in the bubble. Contrary to the barotropic case, where the temperature falls to 10 K at a distance > 10 AU, the radiative feedback extends vertically up to ~ 100 AU with radiative transfer (FLD). Although toroidal magnetic field generation is more effective with HLLD than with LF, the toroidal magnetic field in the FLD-LF case is larger at small radii. This is due to the denser disk formed, which compresses and twists the magnetic lines in the region close to the equatorial plane. At a distance of 100 AU, the toroidal magnetic field component in the vertical direction is one order of magnitude larger with HLLD than with LF. This favors the extension of the magnetic tower. The poloidal magnetic field component is larger everywhere in the HLLD case, since matter is less compressed.

Figure 3 displays the profiles of the magnetic braking at 10 AU above the equatorial plane and in the z -direction at a distance of 10 AU from the center, for the three same calculations. In the equatorial plane, the magnetic braking obtained with the LF solver or in the barotropic case is barely significant. Magnetic braking favors faster accretion on the central object and thus yields a larger amount of kinetic energy to be radiated away at the first core accretion shock (*all* the in-falling gas kinetic energy is radiated away at the first Larson core accretion shock). The gas is then significantly heated up around the central core. In opposite, there is more angular momentum in the (diffusive) FLD-LF case, which promotes fragmentation at the centrifugal barrier. The accretion in the central fragment is thus smaller and the heating due to accretion is less important. Magnetic braking in the z -direction is similar for the three calculations. We thus identify two important processes, both quantitatively affected by the numerical treatment: the presence of a magnetic tower, whose extension depends on the numerical resolution, and the strong magnetic braking in the equatorial plane, whose strength depends on the diffusivity of the solver.

Figure 4 shows the temperature - density distribution for the FLD calculations with the LF solver. The isothermal and adiabatic regimes are recovered at low and high density ($\rho < 10^{-16}$ g cm $^{-3}$ and $\rho > 10^{-12.5}$ g cm $^{-3}$). In between, we observe a dispersion in the (T, ρ) plane, where matter can be hotter at low density and cooler at high density compared with the barotropic treatment (red solid line). As seen in the figure, the fragments eventually reach different isentropes. The central fragment lies on the highest entropy level, while the orbiting fragments end up on cooler isentropes. The barotropic EOS cannot reproduce such a spread in temperature at a given density. The entropy and the minimum Jeans mass in that case are set up by the choice of ρ_{ad} . In the FLD-LF case, cooling is more efficient; material in the equatorial plane cools down by radiating in the vertical directions, where the gas is optically thin. However, this result is mainly affected by the diffusivity of the Riemann solver. In the FLD-HLLD case, all the material has been heated up by the central fragment accretion luminosity and is distributed above the

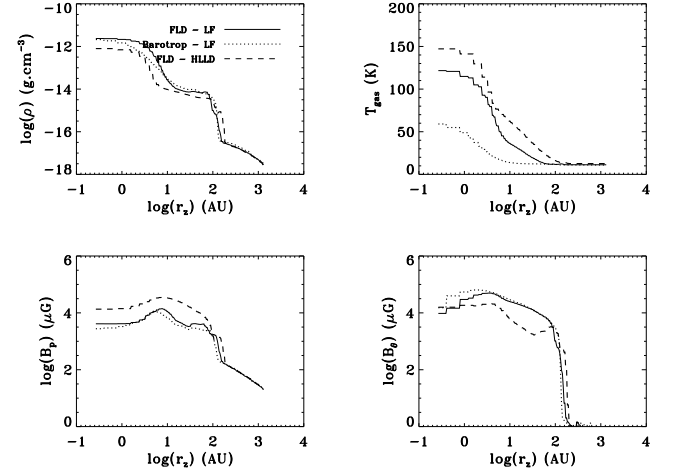


Fig. 2. Case $\mu = 20$: profiles of density (a), temperature (b), poloidal (c) and toroidal (d) magnetic fields in the z -direction at 10 AU from the center, for the same calculations and at the same time as in fig. 1.

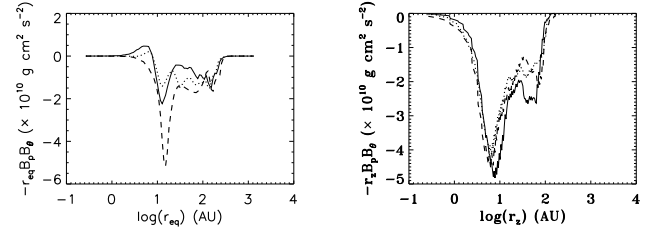


Fig. 3. Case $\mu = 20$: profiles of magnetic braking at 10 AU above the equatorial plane (left) and in the z -direction (right) at a distance of 10 AU from the center, for the same calculations (same legend) and at the same time as in fig. 1.

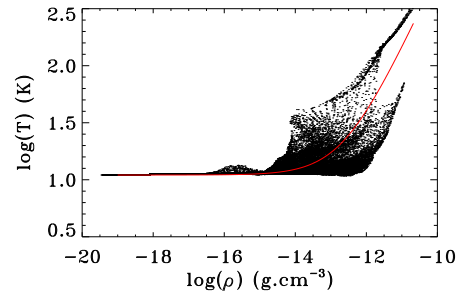


Fig. 4. Case $\mu = 20$: temperature-density plot for each cell in the FLD-LF calculations (black) and with the barotropic EOS (red line).

barotropic adiabat. In the FLD-LF case, the fragmentation is the combined result of the inefficient magnetic braking and of the efficient cooling due to the FLD. This illustrates the great importance and the complexity of the interplay between magnetic field and radiative transfer.

3.2. Case $\mu = 5$

We now consider a strongly magnetized core, with $\mu = 5$, and explore the impact of radiative transfer on the outflow and

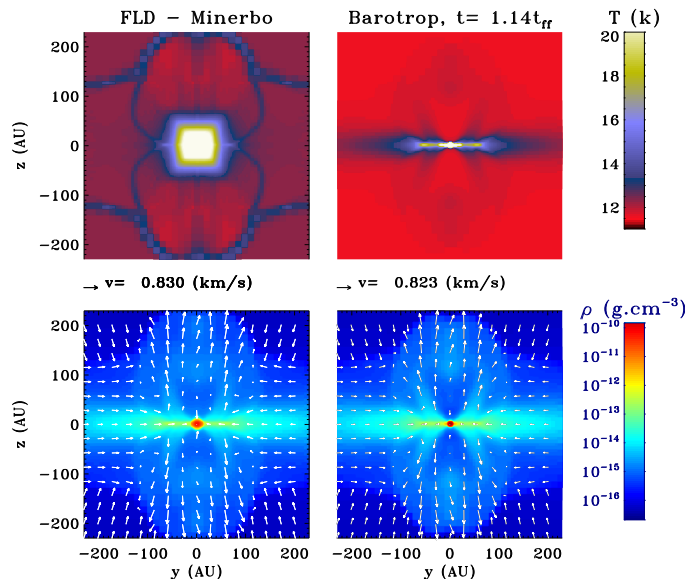


Fig. 5. Case $\mu = 5$: temperature (*top*) and density (*bottom*) maps in the xy -plane for FLD and barotropic EOS calculations (*right*).

on the temperature distribution in that case. Calculations have been performed with the HLLD solver and $N_j = 10$. For this more magnetized model, the magnetic field lines determine the dynamics of the collapse and, contrary to the previous case, it is the flow which adjusts to the magnetic field topology rather than the opposite.

Figure 5 compares temperature and density maps in the yz -plane for the FLD and barotropic calculations, at $t = 1.14 t_{\text{ff}} \sim 38$ kyr. In both cases, an outflow is launched, with similar propagation and opening angles. The density patterns are also similar. The temperature distributions, however, differ drastically. As shown in Hennebelle & Fromang (2008), a pseudo warm disk is formed in the equatorial plane in the barotropic case. Note also the lack of significant heating in the vertical direction with the barotropic EOS. Since the density within the outflow is low, $\rho \sim 5 \times 10^{-15} \text{ g cm}^{-3}$, this implies a low temperature, which quickly falls to 11 K at 10 AU from the center. When including a more proper treatment of radiation, with the FLD, the radiation escapes preferentially in the vertical direction (along the z -axis) and heats up the gas up to about 100 AU. The highest outflow velocity, $v_r \sim 1.4 \text{ km s}^{-1}$, is obtained in the barotropic case while $v_r \sim 1.1 \text{ km s}^{-1}$ in the FLD calculation. The border line between the outflow and the in-falling gas shows a small spike, where the material is shocked and heated. The toroidal magnetic field component profiles are in good agreement with the results of Hennebelle & Fromang (2008) and exhibit a nearly constant plateau in the region of the outflow. For our present study of a $1 M_{\odot}$ core, radiative cooling in the $\mu = 5$ case is found to be almost inconsequential on the collapse. The cores are never found to fragment. For more massive cores with stronger radiative feedback, however, the heating in the outflow is likely to be more dynamically significant (Krumholz et al. 2007).

4. Summary and Discussion

In the present Letter, we have explored the effects of both radiative transfer and magnetic fields (in the limit of ideal MHD) on the fragmentation of a $1 M_{\odot}$ prestellar core. In agreement with the past non-magnetic studies of, for instance, Boss et al.

(2000); Whitehouse & Bate (2006); Krumholz et al. (2007), we show that a proper treatment of radiation is important to correctly describe this process. Radiative transfer enables the gas to significantly cool or heat up in different regions of equal densities whereas a barotropic EOS approximation implies that the cooling and the heating are fixed by the density.

In the case $\mu = 20$, where both the behaviour of the flow and of the magnetic field affect the dynamic of the collapse, we show that radiative transfer has an important impact on the final structure. A barotropic approximation cannot account either for the cooling of the dense and rotating gas in the equatorial plane nor for the heating of the less dense gas in the vertical direction, where radiation is found to escape preferentially. Although a value $\mu = 20$ is not favored by observations, this case clearly illustrates the impact of a proper treatment of radiative transfer on the collapse and fragmentation of prestellar cores. For the strongly magnetized $\mu = 5$ case, the dynamics of the collapse is dominated by the magnetic field. In that case, a proper treatment of radiative cooling is less consequential for the collapse itself but is crucial to derive correct optical depth and temperature distributions, two accessible observational diagnostics. Indeed, the temperature distribution with the FLD is found to strongly depend on the geometry whereas the barotropic approximation yields a nearly uniform distribution. Note also that in the $\mu = 5$ case, we always obtain an outflow, even when using the more diffusive LF Riemann solver. Such outflows can not be obtained presently with SPH calculations. We also performed FLD test calculations including the radiative feedback from a pseudo central newborn star and found that, for our $1 M_{\odot}$ core case, it is inconsequential at the length and time scales of interest.

The spurious diffusivity due to either the numerical resolution or the hydrodynamic solver, however, is found to significantly affect the collapse and the fragmentation. A less diffusive numerical scheme (HLLD instead of LF) produces strong magnetic braking, that transports angular momentum. Material then falls on the central core, leading to a larger accretion luminosity. A good numerical resolution is also crucial in the vertical direction to accurately describe the growth of the magnetic tower, which spreads the gas around the central object.

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Appendix A: Note on the influence of the Riemann solver and of the numerical resolution

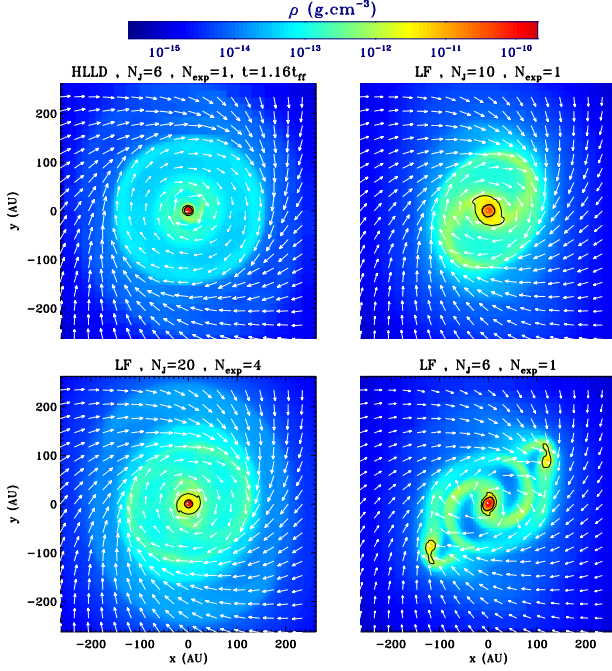


Fig. A.1. Case $\mu = 20$: density maps in the xy -plane at time $t \sim 1.16 t_{\text{ff}}$ for 4 barotropic EOS calculations with HLLD, $N_J = 6$ and $N_{\text{exp}} = 1$; LF, $N_J = 20$ and $N_{\text{exp}} = 4$; LF, $N_J = 10$ and $N_{\text{exp}} = 1$; LF, $N_J = 6$ and $N_{\text{exp}} = 1$.

In this appendix, we present a short convergence study to investigate the effect of both, the Riemann solver and the numerical resolution, on the fragmentation process. We show in section 3.1 that the use of the LF Riemann solver leads to inaccurate results. We perform calculations using the barotropic EOS, and the HLLD or the LF solvers, at various numerical resolution. The latter is determined by 2 parameters: N_J , the number of points per Jeans length, and N_{exp} , that gives the extent of the mesh around a refined cell (if a cell is flagged for refinement, then the N_{exp} cells around the flagged cell, in each direction, will also be refined). A large N_{exp} gives a smoother transition between the levels of the AMR grid. All calculations presented in section 3.1 have been run with $N_{\text{exp}} = 4$. We report results of 4 calculations, run with: HLLD, $N_J = 6$ and $N_{\text{exp}} = 1$; LF, $N_J = 20$ and $N_{\text{exp}} = 4$; LF, $N_J = 10$ and $N_{\text{exp}} = 1$; LF, $N_J = 6$ and $N_{\text{exp}} = 1$.

Figure A.1 portrays the density maps in the equatorial plane for the 4 calculations, at time $t \sim 1.16 t_{\text{ff}}$. The calculations performed with the LF solver, $N_J = 6$ and $N_{\text{exp}} = 1$ clearly diverge from the other ones, since it fragments. The lack of resolution clearly induces inaccurate fragmentation. The three other calculations are qualitatively similar (no fragmentation), and in accordance with Hennebelle & Teyssier (2008) results (obtained using a Roe type Riemann solver). This indicates that the numerical

resolution has to be enhanced with the LF solver in order to avoid spurious effects due to the diffusivity of the solver.

Eventually, note that these differences are more important in the case of FLD calculations, since radiative transfer can have two opposite effects, depending on the strength of the magnetic braking. If the magnetic braking is not significant (with a bad resolution and a diffuse Riemann solver), the material at the centrifugal barrier cools down and then fragments. On the other hand, when the magnetic braking is efficient (with HLLD or a high resolution), the infall velocity and consequently, the accretion luminosity, become larger, which prevents fragmentation to occur (material loses angular momentum and heats up).

Appendix B: Case $\mu = 1000$

For this quasi-hydro case, the initial dense core is highly gravitationally unstable. We have performed three types of calculations with the LF Riemann solver: one with the barotropic EOS and $\gamma = 5/3$, and two with the FLD and different adiabatic exponents ($\gamma = 5/3$ and $\gamma = 7/5$). The value $\gamma = 7/5$ is more appropriate when $T > 100$ K, when the rotational degrees of freedom of H_2 are excited (e.g. Machida et al. 2008). Using $\gamma = 7/5$ yields cooler adiabatic cores than with $\gamma = 5/3$ at the same density. Higher densities and temperatures in the core are thus reached more rapidly.

Figure A.2 portrays density and temperature maps in the equatorial plane for the three aforementioned calculations at a time $t = 1.15 t_{\text{ff}}$. Temperature maps range from 11.4 K to 20 K. As pointed out in Commerçon et al. (2008), the horizon of predictability is very short when the initial thermal support is low. Calculations do not show a convergence to the same fragmentation pattern, since we do not integrate the same system equations. The FLD calculations yield different fragmentation modes for the two different γ 's: with $\gamma = 7/5$, we get a central object and two satellites (4 at later times), whereas with $\gamma = 5/3$, we get a ring fragmentation pattern, with orbiting fragments linked by a bar. The barotropic EOS calculation does not produce a central object. From the temperature map of the FLD case with $\gamma = 7/5$, we see that the central region is quite hot. Fragments are more compressed and they radiate more energy. Fragments are also formed faster than the time required for the radiative feedback to become significant (beginning of the second collapse).

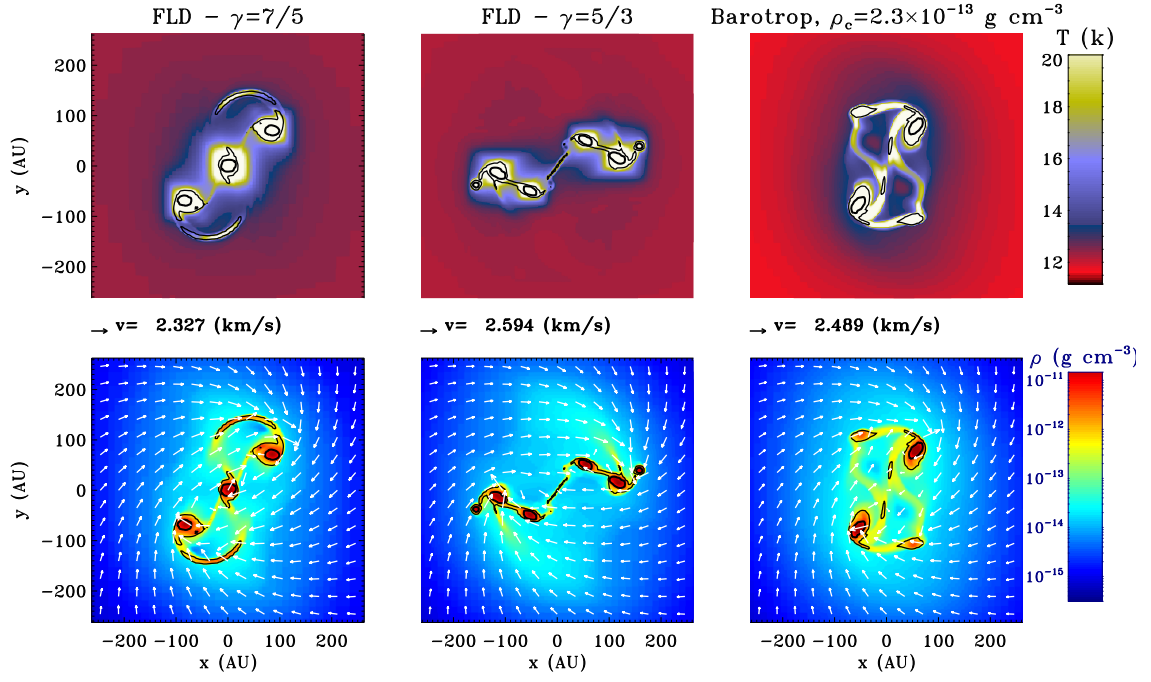


Fig. A.2. Density and temperature maps in the equatorial plane at time $t = 38.3 \text{ kyr}$ ($1.15 t_{\text{ff}}$), for the 3 unmagnetized cases: FLD approximation and $\gamma = 7/5$ (*left*), the FLD approximation and $\gamma = 5/3$ (*middle*) and with a barotropic EOS using $\rho_{\text{ad}} = 2.3 \times 10^{-13} \text{ g cm}^{-3}$ and $\gamma = 5/3$ (*right*). Velocity vectors are over-plotted on the density maps